

INTENSIVE LECTURE SERIES in Mathematics, Keio

Speaker: Prof. Jonathan Sondow



Place: Room 14-216, 2nd Floor, Bldg.14
Yagami Campus, Keio University

Lecture 1 15:30 ~ 16:30 November 13, 2006 (Monday)

New formulas for π and other classical constants

Lecture 2 16:45 ~ 17:45 November 13, 2006 (Monday)

A geometric proof that e is irrational and a new measure of its irrationality

Lecture 3 16:00 ~ 17:00 November 14, 2006 (Tuesday)

An elementary reformulation of the Riemann Hypothesis

I begin with new formulas for π , e , Euler's constant γ , the "alternating Euler constant" $\log 4/\pi$, and the Glaisher-Kinkelin constant A . The formulas involve double integrals, infinite products, hypergeometric series, q -logarithms, and binary expansions of integers. They include a generalization of Ramanujan's integral for γ .

Next I present a simple geometric proof that e is irrational. This leads to a new measure of irrationality for e , that is, a lower bound on the distance from e to a given rational number p/q , as a function of q . Using the integrals for γ and $\log 4/\pi$ (analogous of ones for $\zeta(2)$ and $\zeta(3)$ that Beukers used to simplify Apéry's famous irrationality proof), I give irrationality criteria and conditional irrationality measures for them.

Finally, I use a new formula for the Riemann zeta function to give an elementary reformulation of the Riemann Hypothesis, and of the conjecture that all zeta zeros are simple.

Along the way, I mention several new conjectures. Some results are joint with J. Guillera, P. Hadjicostas, K. Schalm, S. Zlobin, and W. Zudilin.

See my web page <http://home.earthlink.net/~jsondow/> for background reading. First-year students are welcome.